



Tuning and comparing fault diagnosis methods for aeronautical systems via Kriging-based optimization

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Outline

Problem formulation

Tuning methodology

Robust tuning

Summary and future work

Problem formulation

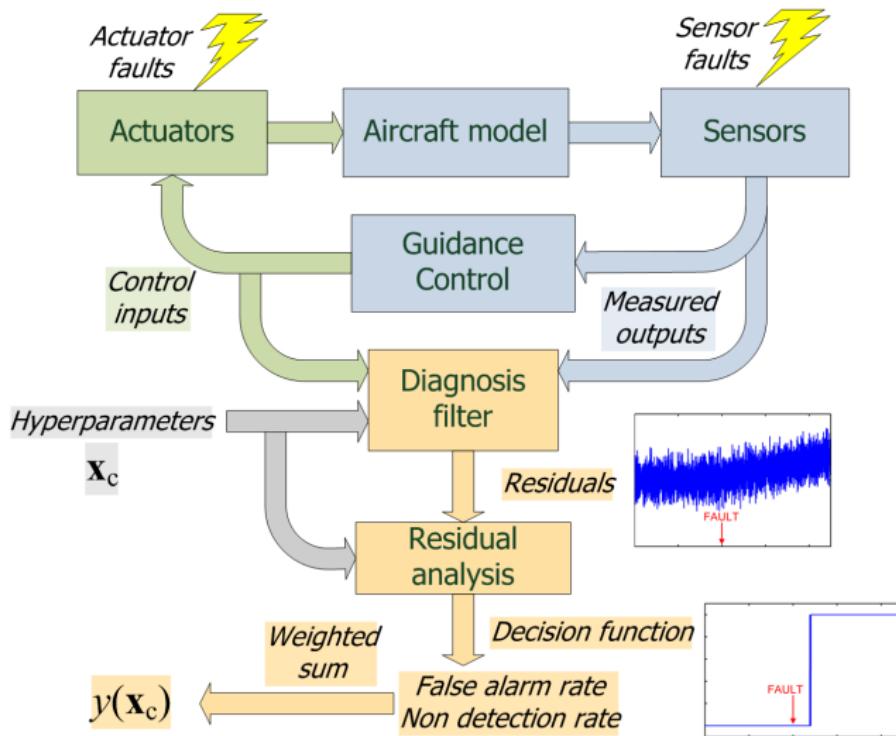
Hyperparameters of fault diagnosis methods

- Observer gains
- Covariance matrices
- Thresholds
- Size of expected change
- Time horizon
- ...

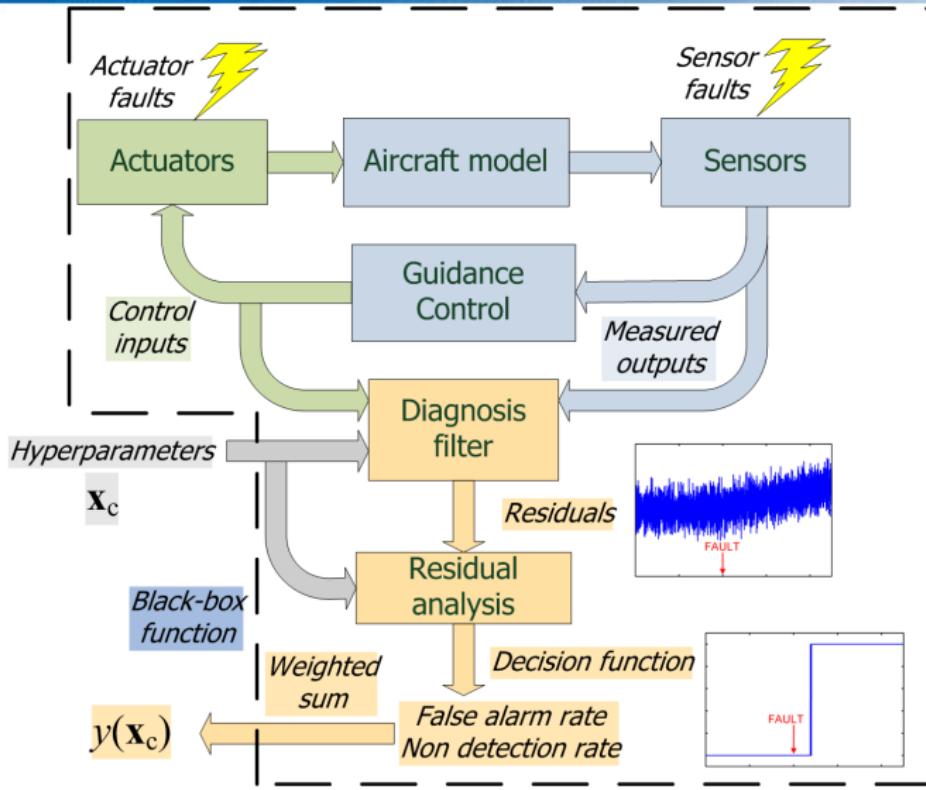
Optimal tuning of Hyperparameters

- Best performance of a method on a complex problem?
- Required to compare fault detection methods
- Involves costly simulations of a test case
- Global minimization of performance indices to find hyperparameters

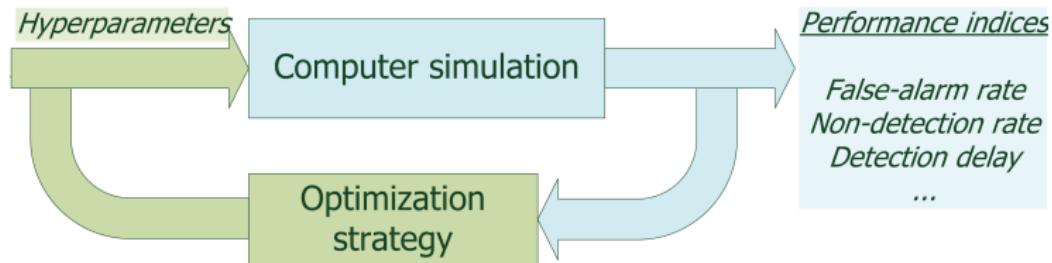
Simulation of a test case : example



Simulation of a test case : example



Problem formulation



Tuning viewed as a *Computer Experiment*

- *Kriging* as a surrogate approximation of the complex simulation
- *Efficient Global Optimization*, iterative search for the global optimizer based on the Kriging prediction

Starting point

Performance index $y(\mathbf{x}_c)$ already computed for an initial sampling of hyperparameter vectors $\mathcal{X}_n = [\mathbf{x}_{c,1}, \dots, \mathbf{x}_{c,n}]$, $\mathbf{x}_c \in \mathbb{X}_c$

Kriging

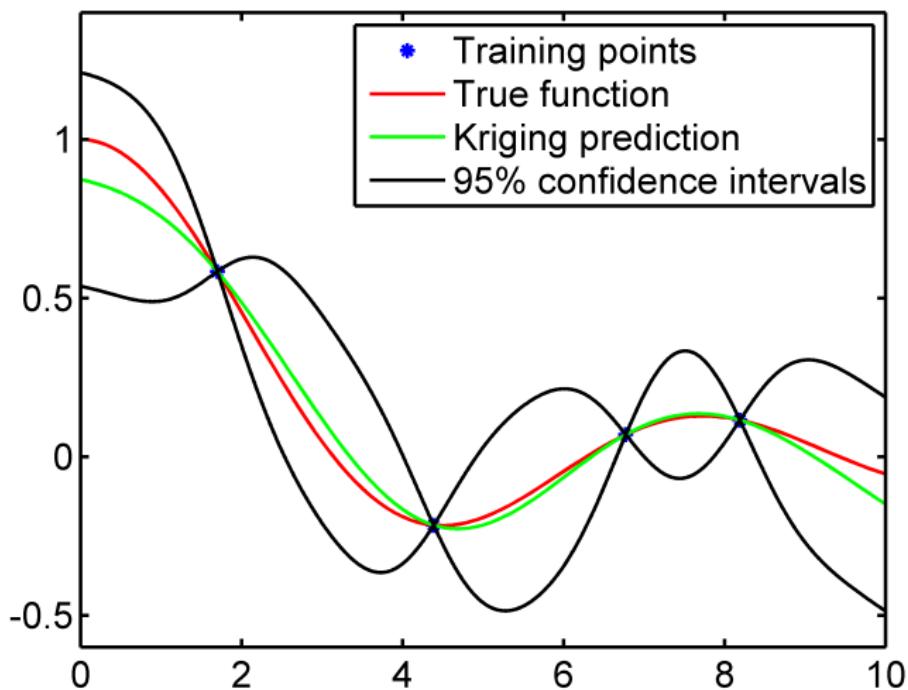
$y(\cdot)$ modeled as a Gaussian process $Y(\mathbf{x}_c) = \mathbf{f}^T \mathbf{b} + Z(\mathbf{x}_c)$ where

- \mathbf{f} parametric prior, \mathbf{b} to be estimated from available data
- $Z(\cdot)$ zero-mean Gaussian process with covariance
 $k(Z(\mathbf{x}_c), Z(\mathbf{x}_c + \mathbf{h})) = \sigma^2 R(\mathbf{h})$
- Chosen correlation function, e.g., $R(\mathbf{h}) = \exp \left\{ - \sum_{k=1}^d \left| \frac{h_k}{\theta_k} \right|^2 \right\}$

What Kriging provides

- $\hat{Y}(\mathbf{x}_c)$, best linear unbiased prediction of $y(\cdot)$ at any $\mathbf{x}_c \in \mathbb{X}_c$
- Variance of the prediction error $\hat{\sigma}^2(\mathbf{x}_c)$

Kriging illustration



Efficient Global Optimization (EGO) algorithm

Objective: find iteratively the minimum of $y(\cdot)$

- ① Choose an initial sampling and compute the value of $y(\cdot)$ at those points
- ② Find the empirical minimum in the available data points, y_{\min}
- ③ Fit a Kriging predictor on those data points
- ④ Find a new point of interest to evaluate $y(\cdot)$ by maximizing Expected Improvement, given by

$$EI(x_c) = \hat{\sigma}(x_c) [u\Phi(u) + \phi(u)]$$

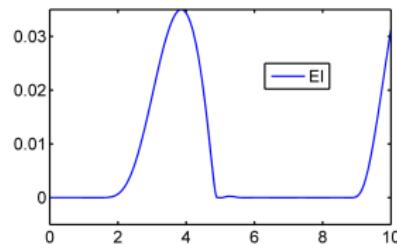
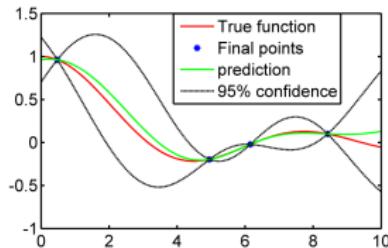
where

$$u = \frac{(y_{\min} - \hat{Y}(x_c))}{\hat{\sigma}(x_c)}$$

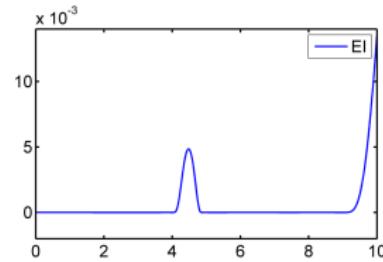
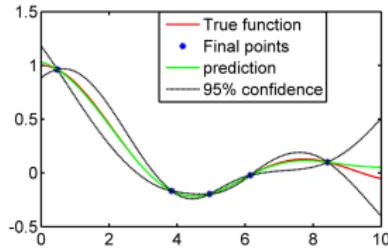
- ⑤ Go to step 2 until EI reaches a threshold or sampling budget is exhausted

Illustration of EGO

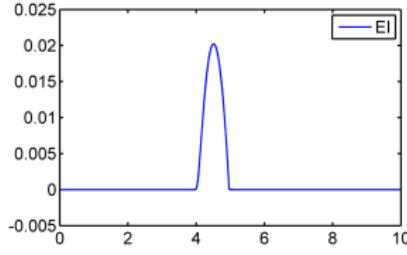
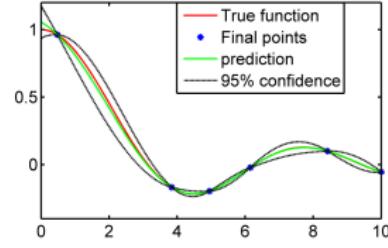
Iteration 1



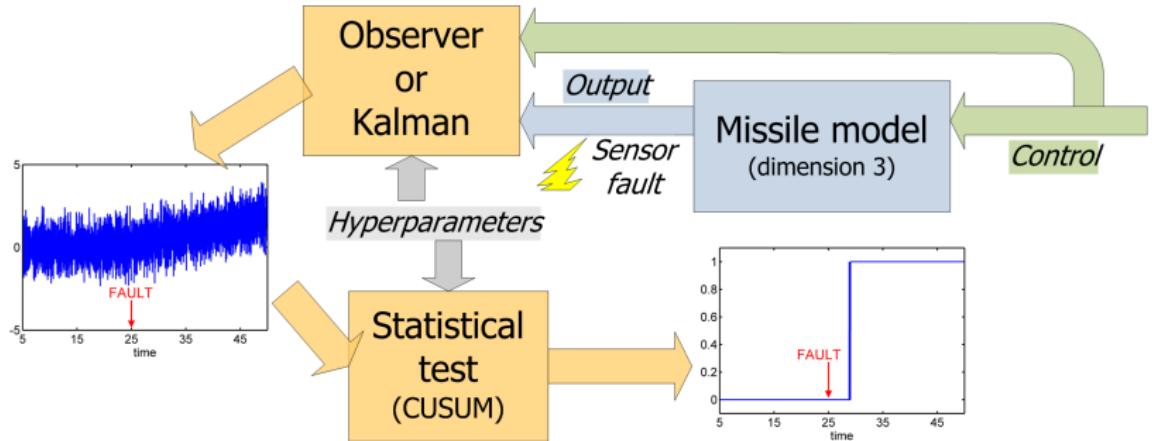
Iteration 2



Iteration 3

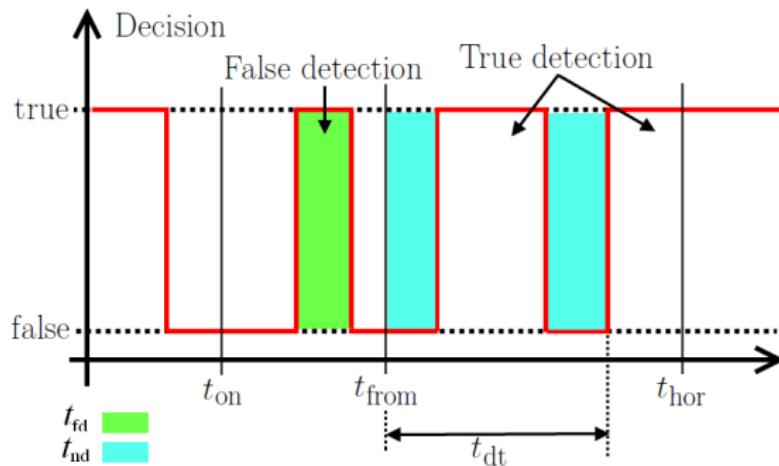


Application – tuning of 2 fault-diagnosis schemes



- ① Luenberger observer (3 poles) + CUSUM (2 hp) → 5 hp
- ② Kalman filter (4 non-zero initial covariance values)
+ CUSUM (2 hp) → 6 hp

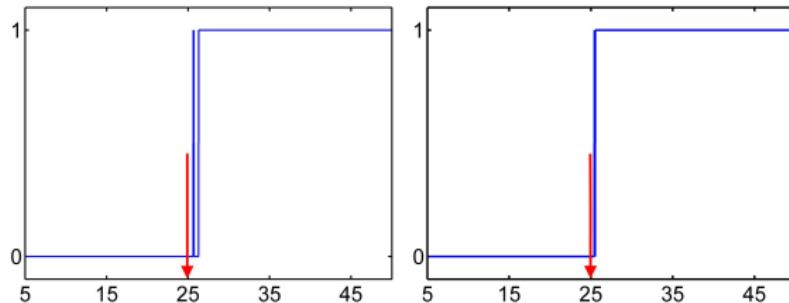
Cost function



$$r_{fd} = \frac{t_{fd}}{t_{from} - t_{on}}, \quad r_{nd} = \frac{t_{nd}}{t_{hor} - t_{from}} \rightarrow y = r_{fd} + r_{nd}$$

$$\hat{\mathbf{x}}_c = \arg \min_{\mathbf{x}_c \in \mathbb{X}_c} y(\mathbf{x}_c)$$

A sample of numerical results

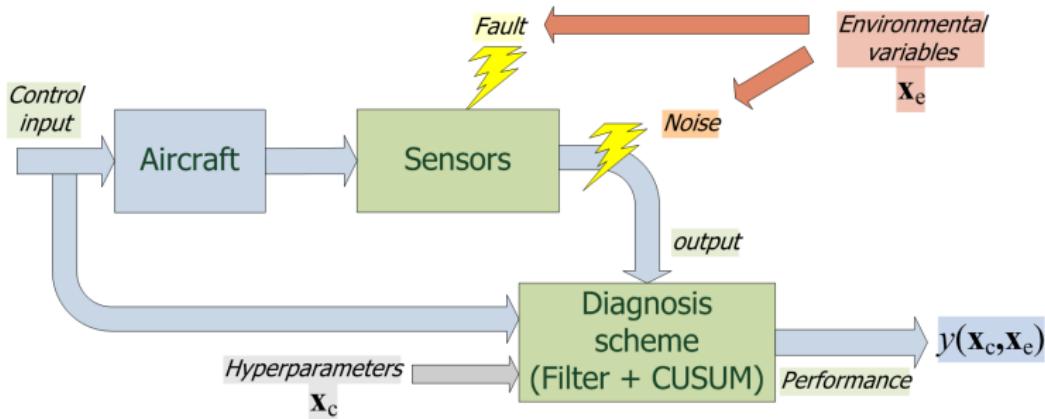


	Observer and CUSUM	Kalman and CUSUM
<i>Ranking</i>	2	1
False-alarm rate	0	0
Non-detection rate	0.0455	0.0184
Mean number of simulations	102.21	136.14

Robust tuning

Need for a robust tuning

- Results obtained for fixed conditions of the simulation
- What happens with stronger disturbances, more noise, smaller fault ?
- → Simulation depends on a set of *environmental variables* \mathbf{x}_e



Robust tuning – proposed solution

Continuous minimax optimization

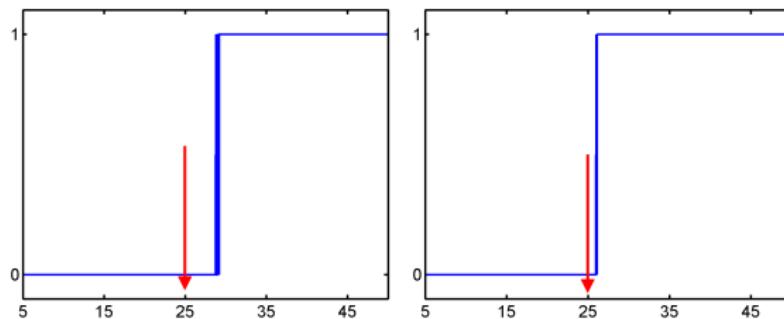
- Search for optimal tuning for worst-case environmental variables

$$\hat{\mathbf{x}}_c, \hat{\mathbf{x}}_e = \arg \min_{\mathbf{x}_c \in \mathbb{X}_c} \max_{\mathbf{x}_e \in \mathbb{X}_e} y(\mathbf{x}_c, \mathbf{x}_e)$$

Sketch of proposed algorithm

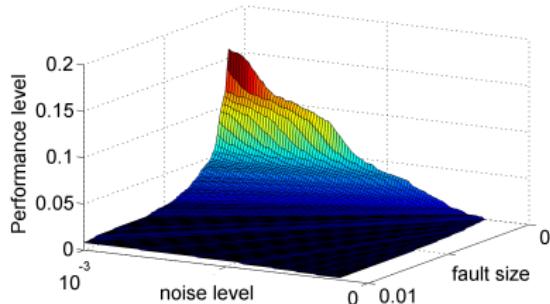
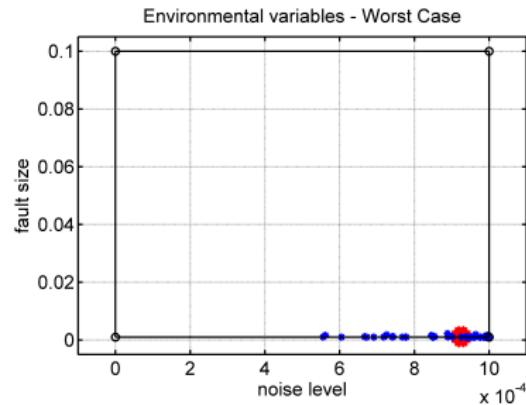
- Transform the initial problem into
$$\begin{cases} \min_{\mathbf{x}_{c,\tau}} \tau \\ y(\mathbf{x}_c, \mathbf{x}_e) < \tau, \forall \mathbf{x}_e \end{cases}$$
- Iterative relaxation :
 - Draw a new \mathbf{x}_e
 - Find a minimum $\hat{\mathbf{x}}_c$ for all explored \mathbf{x}_e with EGO
 - Find a maximum $\hat{\mathbf{x}}_e$ for $\hat{\mathbf{x}}_c$ with EGO
 - Check convergence, repeat if necessary

Robust tuning for aircraft fault diagnosis application



	Observer and CUSUM	Kalman and CUSUM
Ranking	2	1
Minimax performance	0.114	0.0312
Average number of simulations	168	199

Worst-case estimation



Summary and future work

Summary

- Automatic tuning with *Kriging* and *Bayesian Optimization*
- Tuning complete FDI schemes for dynamical systems : simultaneous adjustment of hyperparameters of residual-generation and residual-evaluation strategies
- Robust tuning algorithm in the worst-case sense
- Few runs of the simulation required (20 to 30 per dimension)
- Generic : applicable to many engineering design problems

Future work

- Consider higher-dimensional problems (in both dimensions)
- More complex constraints on the cost function